

Задача № 16.

Найти НОД многочленов с помощью алгоритма Евклида.

1.

$$f(x) = x^6 - 2x^3 - 4x^2 - 8x - 3,$$

$$g(x) = 3x^4 - 4x^3 + 8x^2 - 5x - 4;$$

2.

$$f(x) = x^7 + 3x^6 - 11x^5 + 15x^2 + 2x + 10,$$

$$g(x) = x^6 + 5x^5 - x^4 - 3x^3 - 10x^2 - x - 5;$$

3.

$$f(x) = -12x^5 + 28x^4 - 17x^3 - 27x^2 + 22x - 4,$$

$$g(x) = -6x^2 + 5x - 1;$$

4.

$$f(x) = 14x^6 - 24x^5 + 38x^4 + 15x^3 - 123x^2 + 56x + 10,$$

$$g(x) = 14x^4 - 24x^3 + 66x^2 - 33x - 5;$$

5.

$$f(x) = 3x^5 + 4x^4 - 4x^3 - 6x^2 + x + 2,$$

$$g(x) = 3x^4 + 7x^3 - 7x - 3;$$

6.

$$f(x) = 2x^5 + 21x^4 + 51x^3 - 41x^2 - 47x + 26,$$

$$g(x) = 2x^4 + 23x^3 + 72x^2 + 20x - 31;$$

7.

$$f(x) = 3x^5 + 3x^4 - 3x^3 - 6x - 3,$$

$$g(x) = 3x^4 + 2x^3 + x^2 + 2x - 2;$$

8.

$$f(x) = 3x^6 - 21x^4 + 24x^3 - 21x + 21,$$

$$g(x) = 3x^5 - 7x^3 + 3x^2 - 7;$$

9.

$$f(x) = 3x^5 + 5x^4 + 6x^3 + 6x^2 + 2x + 1,$$

$$g(x) = x^3 + x^2 + x + 1;$$

10.

$$f(x) = -4x^4 + x^3 + x^2 + 15x - 13,$$

$$g(x) = 2x^4 - 7x + 5;$$

11.

$$f(x) = -10x^4 - x^3 - 10x^2 + 14x + 7,$$

$$g(x) = -2x^4 - 2x^2 + 3x + 1;$$

12.

$$f(x) = x^4 + x^3 - 3x^2 + 2x - 1,$$

$$g(x) = x^3 - 3x^2 + 5x - 3;$$

13.

$$f(x) = 4x^5 + 2x^4 + 4x^3 + 11x^2 - 4x + 3,$$

$$g(x) = 4x^4 + 2x^3 + 9x;$$

14.

$$f(x) = x^5 + 2x^4 - 4x^3 - x^2 + 6x - 4,$$

$$g(x) = x^4 + 3x^3 - x^2 - 3x + 2;$$

15.

$$f(x) = x^5 - 4x^4 - 31x^3 + 125x^2 - 100x + 384,$$

$$g(x) = \frac{1}{2}x^3 - 2x^2 - 17x + 68$$

16.

$$f(x) = 3x^5 + 4x^4 - 4x^3 - 6x^2 + x + 2,$$

$$g(x) = 3x^4 + 7x^3 - 7x - 3;$$

17.

$$f(x) = 2x^5 + x^3 + 2x^2 - 6x - 3,$$

$$g(x) = 2x^4 - 2x^3 - x^2 + 3x - 3;$$

18.

$$f(x) = 2x^6 + 2x^5 + 2x^4 + 7x^3 + 2x^2 + 4x + 5,$$

$$g(x) = 2x^5 + 2x^4 + 4x^3 + 5x^2 + 2;$$

19.

$$f(x) = x^5 - 2x^4 + x^3 + x - 1,$$

$$g(x) = x^4 - 2x^3 + x^2 - x + 1;$$

20.

$$f(x) = 2x^5 - 4x^4 - 4x^3 - x^2 + x - 1,$$

$$g(x) = x^4 - 3x^3 + x^2 - x - 2;$$

21.

$$f(x) = x^5 - 3x^4 + 3x^3 - x^2 - 2x + 2,$$

$$g(x) = x^4 + 2x^3 - 3x^2 - x + 1;$$

22.

$$f(x) = 4x^5 + x^4 - 3x^3 + 2x^2 - 6x + 5,$$

$$g(x) = 4x^4 + x^3 + 10x;$$

23.

$$f(x) = x^5 - 7x^4 + 19x^3 - 25x^2 + 16x - 4,$$

$$g(x) = x^4 - 3x^3 + 3x^2 - x;$$

24.

$$f(x) = 3x^5 + 2x^4 + 4x^3 - x^2 - 4x + 8,$$

$$g(x) = x^4 - x^3 + 2x^2 - 2x - 4;$$

25

$$f(x) = 2x^5 + 3x^4 - 13x^3 - 10x^2 + 21x + 6,$$

$$g(x) = 2x^4 + 5x^3 - 8x^2 - 19x + 2;$$

26.

$$f(x) = x^5 + 3x^4 + 2x^3 + 6x^2,$$

$$g(x) = x^4 + 2x^3 - 3x^2 + 4x;$$

27.

$$f(x) = 12x^5 - 34x^4 - 15x^3 + 16x^2 - 5x - 5,$$

$$g(x) = 12x^4 - 22x^3 + 19x^2 + x + 7;$$

28.

$$f(x) = x^5 - 8x^4 + 2x^3 - 5x^2 + 3x - 1,$$

$$g(x) = x^4 - 2x^3 + 4x^2 - x + 2;$$

29.

$$f(x) = x^5 + 5x^4 + 3x^3 - 9x^2,$$

$$g(x) = x^4 + 3x^3 + 3x^2 + 9x;$$

30.

$$f(x) = 4x^5 - 6x^4 + 10x^3 - 7x^2 + 2x - 3,$$

$$g(x) = 2x^4 - 3x^3 + 4x^2 - 2x - 1;$$

31.

$$f(x) = x^5 + x^4 - 3x^3 + 9x^2,$$

$$g(x) = x^4 + 2x^3 - 8;$$

32.

$$f(x) = 2x^6 + 3x^5 - 12x^4 + 22x^3 - 9x^2 - 11x - 5,$$

$$g(x) = 2x^4 + 5x^3 - 11x^2 - x + 5;$$

33.

$$f(x) = x^6 - 7x^5 + x^4 - 2x^3 - 35x^2 + 5x - 35,$$

$$g(x) = x^4 - 7x^2 + x - 7;$$

34.

$$f(x) = x^6 + 3x^5 + 3x^4 + 7x^3 + 3x^2 + 4x + 1,$$

$$g(x) = x^4 + 3x^3 + 2x^2 + 4x + 1;$$

35.

$$f(x) = x^6 - 4x^5 + 14x^4 - 38x^3 + 49x^2 - 75x + 25,$$

$$g(x) = x^4 - 4x^3 + 7x^2 - 11x + 5;$$

36.

$$f(x) = -2x^6 + 4x^5 + 9x^4 - 19x^3 - 6x^2 + 15x + 2,$$

$$g(x) = -2x^4 + 4x^3 + 5x^2 - 9x - 2.$$

Дополнительно:

1) $x^5 + x^3 + x^2 + 2x + 1$, $x^5 + 2x^4 + x^3 + 1$ над полем Z_3 ;

2) $x^5 + x^3 + x^2 + 2x + 1$, $x^5 + 2x^4 + x^3 + 1$ над полем Q .

3) $x^5 + 4x^4 + 3x^3 + x^2 + 4$ и $x^4 + 4x^3 + 4x^2 + 4$ над полем Z_3 ;

4) $x^5 + 4x^4 + 3x^3 + x^2 + 4$ и $x^4 + 4x^3 + 4x^2 + 4$ над полем Z_5 ;

5) $x^5 + 4x^4 + 3x^3 + x^2 + 4$ и $x^4 + 4x^3 + 4x^2 + 4$ над полем Q .

6) $x^5 - x^4 - 2x^3 + 2x^2 + 9x - 9$ и $x^5 + x^4 + 4x^3 - x^2 + x - 6$ над полем Z_3 ;

7) $x^5 - x^4 - 2x^3 + 2x^2 + 9x - 9$ и $x^5 + x^4 + 4x^3 - x^2 + x - 6$ над полем Z_5 ;

8) $x^5 - x^4 - 2x^3 + 2x^2 + 9x - 9$ и $x^5 + x^4 + 4x^3 - x^2 + x - 6$ над полем Z_7 ;

9) $x^5 - x^4 - 2x^3 + 2x^2 + 9x - 9$ и $x^5 + x^4 + 4x^3 - x^2 + x - 6$ над полем Q .